

Hero's Square Roots

Suppose you want the square root of N . You guess an initial value, X_0 and calculate a better value, X_1

$$X_1 = (X_0 + N/X_0)/2$$

Then you use X_1 as your next guess and calculate a better guess, X_2 :

$$X_2 = (X_1 + N/X_1)/2$$

And so on $X_3=, X_4.....$ etc.

For an example we want to know the square root of 10. We know that 3 squared is 9 and 4 squared is 16 so may be for X_0 we could try 3.5. However what about any other number? So I suggest we always start with the number 1. That is we guess the square root of any number is 1. Not very clever but it just means a few more guesses before we get the answer we want. Possibly an extra 1/100 of a second computing time – so who cares then!



tries	
1	1
2	5.5
3	3.659091
4	3.196005
5	3.162456
6	3.162278

+ length: 6

So the first guess gives us $X_1 = (1+10/1)/2 = 11/2 = 5.5$

Then $X_2 = (5.5+10/5.5)/2 = 3.659091$

etc.

Try your own ideas before looking at the next crib.....



```
when clicked
  change error by 1e-11
  set sqrt to 0
  delete all of tries
  ask Square root off and wait
  set rootis to 0
  if answer = why and what goes here then
  if answer < why and what goes here then
  sqrt answer
```

```
define sqrt number
  set sqrt to 1
  repeat until why and what goes here < why and what goes here
  set sqrt to (sqrt + number / sqrt) / 2
  say join join square root of answer is for 5 secs
```